

Class 9 maths - chapter 1

Number System : Laws of Exponents (concept and Mcq's)

$$\frac{a^m \cdot a^n}{(a)^{m+n}}$$

$$5^2 \cdot 5^3 = 5^{2+3} = 5^5$$

$$\frac{(a^m)^n}{a^{mn}}$$

$$\frac{[(2)^3]^2}{(2)^{3 \times 2}} = 2^6$$

$$\frac{(a)^m}{(a)^n} = (a)^{m-n}$$

Base same →
Powers add.
(Power) Power
→ Multiply.

Base same - divide
→ Powers
Subtract

$$\frac{2^4}{2^3} = 2^{4-3} = 2^1 = 2.$$

$$a^m b^m = (ab)^m$$

$$\frac{a^m}{b^m} = \left(\frac{a}{b}\right)^m$$

NCERT Expt 2 (i) $2^{\frac{2}{3}} \cdot 2^{\frac{1}{3}} = (2)^{\frac{2}{3} + \frac{1}{3}} = 2^{\frac{2+1}{3}} = 2^{\frac{3}{3}} = 2^1 = 2$

(ii) $\{(3)^{\frac{1}{5}}\}^4 = (3)^{\frac{1}{5} \times 4} = (3)^{\frac{4}{5}}$

(iii) $\frac{7^{\frac{1}{5}}}{7^{\frac{1}{3}}} = (7)^{\frac{1}{5} - \frac{1}{3}} = (7)^{\frac{3-5}{15}} = (7)^{-\frac{2}{15}}$

(iv) $(13)^{\frac{1}{5}} \cdot (17)^{\frac{1}{5}} = (13 \times 17)^{\frac{1}{5}} = (221)^{\frac{1}{5}}$

On simplifying $8^3 \times 2^4$, we get

(a) 16^7

(b) 2^{13}

(c) 2^{10}

(d) 8^4

$$8^3 \times 2^4 \\ [(2)^3]^3 \times 2^4$$

$$(2)^{3 \times 3} \times 2^4 = 2^9 \times 2^4 = 2^{9+4}$$

$$\begin{array}{r} 2 | 8 \\ 2 | 4 \\ 2 | 2 \\ \hline 1 \end{array}$$

$$= 2^{13}$$

13 x 17
3 7

$$\begin{array}{r} 200 \\ 21 \\ \hline 221 \end{array}$$

$(16)^{3/4}$ is equal to

- (a) 2 (b) 4 ✓ (c) 8

- (d) 16

$$\begin{aligned} & (16)^{\frac{3}{4}} \\ & \left\{ (2^4)^{\frac{3}{4}} \right. \\ & (2)^{4 \times \frac{3}{4}} = 2^3 = 8 \end{aligned}$$

2	16
2	8
2	4
2	2
2	1

Value of $(256)^{0.16} \times (256)^{0.09}$ is

(A) 4

(B) 16

(C) 64

(D) 256.25

$$(256)^{0.16} \times (256)^{0.09}$$

$$(256)^{0.16 + 0.09} = (256)^{0.25}$$

$$(256)^{\frac{25}{100}} = (256)^{\frac{1}{4}}$$

$$\left\{ (2)^8 \right\}^{\frac{1}{4}}$$

$$= 2^{\frac{8 \times 1}{4}} = 2^2 = 4$$

$$\begin{array}{r|rr} 2 & 256 \\ \hline 2 & 128 \\ \hline 2 & 64 \\ \hline 2 & 32 \\ \hline 2 & 16 \\ \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

$\sqrt[4]{\sqrt[3]{2^2}}$ equals

(A) $2^{-\frac{1}{6}}$

(B) 2^{-6}

(C) $2^{\frac{1}{6}}$

(D) 2^6

$$\left(\left((2)^2 \right)^{\frac{1}{2}} \right)^{\frac{1}{4}}$$

$$(2)^{2 \times \frac{1}{3} \times \frac{1}{4}} = 2^{\frac{1}{6}}$$

$$\sqrt{a} = a^{\frac{1}{2}}$$

$$\sqrt[3]{a} = a^{\frac{1}{3}}$$

$$\sqrt[4]{a} = a^{\frac{1}{4}}$$

$$\sqrt[5]{a} = a^{\frac{1}{5}}$$

Value of $\sqrt[4]{(81)^{-2}}$ is

(A) $\frac{1}{9}$

(B) $\frac{1}{3}$

(C) 9

(D) $\frac{1}{81}$

$$[(81)^{-2}]^{\frac{1}{4}}$$

$$(81)^{-2 \times \frac{1}{4}} = (81)^{-1/2}$$

$$(9 \times 9)^{-1/2} = [(9^2)^{-1}]^{1/2} = (9)^{2 \times -\frac{1}{2}}$$

$$= 9^{-1} = \frac{1}{9}$$

The $\sqrt[3]{a}$ cube root of 125 divided by \sqrt{a} square root of 25, is

- a) 5
- b) 1
- c) $1/5$
- d) None of these

$$\sqrt[3]{a} = (a)^{\frac{1}{3}}$$

$$\sqrt{a} = (a)^{\frac{1}{2}}$$

$$\frac{\sqrt[3]{125}}{\sqrt{25}} = \frac{\left[(5)^3\right]^{\frac{1}{3}}}{\left[(5)^2\right]^{\frac{1}{2}}}$$

$$\begin{array}{r} 5 \\ \sqrt[3]{125} \\ \hline 5 | 25 \\ 5 | 25 \\ \hline 5 \end{array}$$

$$\frac{(5)^{3 \times \frac{1}{3}}}{5^{2 \times \frac{1}{2}}} = \frac{5}{5} = 1.$$

The value of $\{-3/8\}^{-3} \times \{4/9\}^{-2}$ is:

(A) -96

(B) $\frac{-8192}{2187}$

(C) $\frac{4}{96}$

(D) $\frac{-1}{192}$

$$\left(\frac{-3}{8}\right)^{-3} \times \left(\frac{4}{9}\right)^{-2}$$

$$\left(\frac{a}{b}\right)^{-3} = \left(\frac{b}{a}\right)^3$$

$$\left(\frac{-8}{3}\right)^3 \times \left(\frac{9}{4}\right)^2$$

$$\frac{\cancel{-8}^2 \times \cancel{-8}^2}{\cancel{8}^1 \times \cancel{3}^1} \times \frac{\cancel{9}^3}{\cancel{4}^1} = -96$$