

Calculus 1

Find glb and lub of the set.

$$\left\{ \frac{1}{2+x^2} ; -6 \leq x \leq 4 \right\}$$

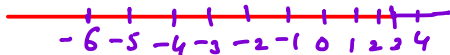
$$y = \frac{1}{2+x^2}$$

$$-6 \leq x \leq 4 < 6$$

$$-6 \leq x < 6$$

$$|x| \leq 6$$

$$x^2 \leq 36 \quad \text{--- ①}$$



$$x^2 \geq 0 \quad \text{--- (11)}$$

from (7) + (11)

$$0 \leq x^2 \leq 36$$

$$2 \leq 2 + x^2 \leq 38$$

$$\frac{1}{2} \geq \frac{1}{2 + x^2} \geq \frac{1}{38}$$

$$\frac{1}{38} \leq \frac{1}{2 + x^2} \leq \frac{1}{2}$$

$$\text{l.u.b} = \frac{1}{2}$$

$$\text{g.l.b} = \frac{1}{38}$$