

Calculus - 1

Properties of Real Numbers and Bounds : lecture 5

Bounds,greatest lower bound and least upper bound

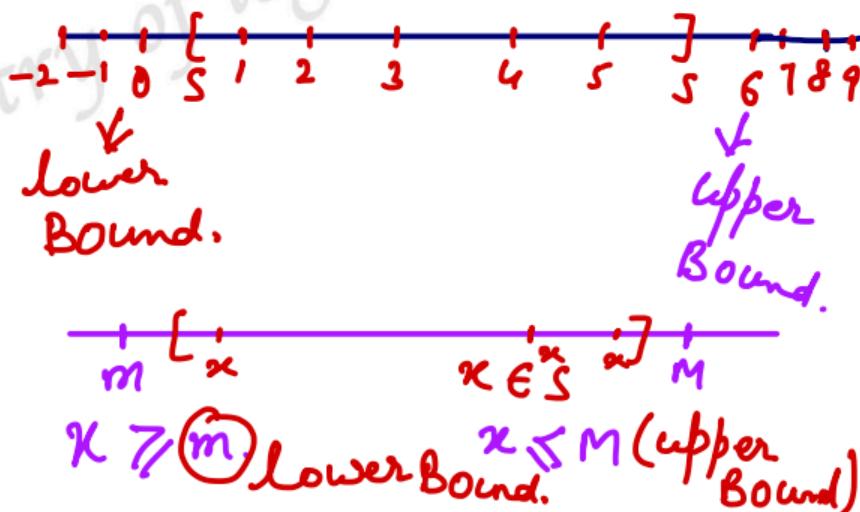
$$S = \{1, 2, 3, 4, 5\}$$

$x \in S$.

$x \leq M$.

M is Upper Bound.

S is Bounded above



$x \geq m.$

m is lower Bound.

S is Bounded Below.

$m \leq x \leq M.$

A set which is Bounded Below and Bounded above is Bounded.

g.l.B :Greatest lower Bound.

→ Inf and Sup. Value of a set is unique.

→ Order completeness property.

Set of Bounded above then supremum exists.

A set is Bound Below

then infimum exists.



$\nearrow M$

M, M_2, M_3

least upper bound.

(Supremum)

find l.u.b and g.l.b.

$$S = \frac{2x-1}{x+4} \quad |x-5|=2$$

$$S = 2 - \frac{9}{x+4}$$

$$|x-5|=2$$

$$-2 < x-5 < 2$$

$$-2+5 < x < 2+5$$

$$3 < x < 7$$

$$3+4 < x+4 < 7+4$$

$$7 < x+4 < 11$$

$$\frac{1}{7} > \frac{1}{x+4} > \frac{1}{11}$$

$$\frac{-9}{7} < \frac{-9}{x+4} < \frac{-9}{11}$$

$$2 - \frac{9}{7} < 2 - \frac{9}{x+4} < 2 - \frac{9}{11}$$

$$\frac{5}{7} < \frac{2x-1}{x+4} < \frac{13}{11}$$

$$\frac{5}{7} \qquad \qquad \qquad \frac{13}{11}$$

Inf. G.L.b $\rightarrow \frac{5}{7}$
Supremum: L.U.b $\rightarrow \frac{13}{11}$