

Preparation for CSIR NET | IIT JAM | GATE

Continuity and Differentiability : Short Trick

$$f(x) = \begin{cases} x^\alpha \sin\left(\frac{1}{x^\beta}\right) & : x \neq 0 \\ 0 & x = 0 \end{cases}$$

- (i) $f(x)$ is differentiable at $x=0$ iff $\alpha > 1$
- (ii) $f(x)$ is continuous at $x=0$ iff $\alpha > 0$



OMG! MATHS!
The poetry of logical ideas.

$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$$

Then $f(x)$ at $x=0$.

(a) limit does not exist.

(b) Continuous and differentiable

(c) Continuous but not differentiable.

(d) None of these.

$$f(x) = \begin{cases} \sqrt{x} \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$$

then $f(x)$ is at $x=0$.

- (a) limit does not exist.
- (b) Continuous and differentiable
- ~~(c)~~ Continuous but not differentiable.
- (d) None of these.

$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$$

then $f(x)$ is at $x=0$

(a) limit does not exist.

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$$f(x) = \begin{cases} x^3 \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases} \quad \text{then } f(x) \text{ at } x=0 \text{ is.}$$

- (a) limit does not exist
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- (c) Continuous but not differentiable.
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